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(Assignment - 4) (Unit - 4)

1- Determine base of the following.

(i) $(345)_{10} = (531)_x$

$$\begin{array}{ccccccc} & & 3 & 4 & 5 & & \\ & & 10^2 & 10^1 & 10^0 & & \\ & & & & & x^2 & x^1 & x^0 \end{array}$$

$$\Rightarrow 3 \times 10^2 + 4 \times 10^1 + 5 \times 10^0 = 5x^2 + 3x^1 + 1x^0$$

$$\Rightarrow 300 + 40 + 5 = 5x^2 + 3x^1 + 1$$

$$5x^2 + 3x^1 - 344 = 0 \quad \text{--- (A)}$$

Suppose we take $x = 8$ then put into eq (A)

$$5(8)^2 + 3(8) - 344 = 0$$

$$5 \times 64 + 24 - 344 = 0$$

$$344 - 344 = 0$$

$$0 = 0$$

Now

$$(345)_{10} = (531)_8$$

(ii) $(2374)_{16} = (9076)_x$

$$\Rightarrow 2 \times 16^3 + 3 \times 16^2 + 7 \times 16^1 + 4 \times 16^0 = 9x^3 + 0x^2 + 7x^1 + 6x^0$$

$$8192 + 768 + 112 + 4 = 9x^3 + 7x + 6$$

$$9076 = 9x^3 + 7x + 6$$

$$9x^3 + 7x - 9070 = 0 \quad \text{--- (A)}$$

Assume $x = 10$; put $x = 10$ in eq (A)

$$9(10^3) + 7(10) - 9070 = 0$$

$$9000 + 70 - 9070 = 0$$

$$0 = 0$$

then $(2374)_{16} = (9076)_{10}$

(iii) Subtract using 10's Complement:

$$(9754)_{10} - (364)_{10}$$

Suppose $A = 9754$ $B = 364$

find $A - B = ?$ Using 10's Complement

find 10's Comp. of $B = 364$

10's Comp of a no is 1 add to

9's Comp. no. 9999

9's Comp. of 364 is 364

9635

then add 1

+1

9636

Now add 9636 with A

9754

+ 9636

19390

Carry

then

$$(9754)_{10} - (364)_{10} = (9390)_{10}$$

(iv) Subtract using 1's Comp. $(10111)_2 - (110011)_2$

we have $A = 10111$ and $B = 110011$

First we obtain 1's Comp of $B = 110011$

then we add A and 1's Comp of B

$A = 10111$

1's Comp of B + 001100

Zero final carry $\boxed{0} 100011 \leftarrow$ Final Answer

then we invert the final answer.

Since the final ans is in 1's Comp form we have to invert it to obtain the true ans.

thus $100011 \xrightarrow{\text{invert}} 011100 = (28)_{10}$

Hence the answer is $\boxed{- (28)_{10}}$ Ans

(v) $(2CCD)_{16} = (\quad)_{8} = (\quad)_{5}$

In Hexadecimal $\rightarrow ()_{16}$

Hexadecimal

0010110011001101

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow \quad \downarrow$

$0 \quad 2 \quad 6 \quad 3 \quad 1 \quad 5 \Rightarrow (026315)_8$

$(026315)_8 \rightarrow ()_5$

$$\Rightarrow 0 \times 8^5 + 2 \times 8^4 + 6 \times 8^3 + 3 \times 8^2 + 7 \times 8^1 + 5 \times 8^0$$

$$\Rightarrow (11469)_{10}$$

$(11469)_{10} \rightarrow (\quad)_5$

$$\begin{array}{r|l}
 5 & 11469 \\
 \hline
 5 & 2293 \quad 14 \\
 \hline
 5 & 458 \quad 13 \\
 \hline
 5 & 91 \quad 13 \\
 \hline
 5 & 18 \quad 13 \\
 \hline
 & 3 - 13 \\
 & \uparrow \\
 & M6B
 \end{array}$$

$$\Rightarrow (337334)_5$$

Q. State De Morgan's Law?

Answer • De Morgan's law $\rightarrow$ there are two de-Morgan's law.

1. Two separate term NORed together is the same as two term inverted (Complement) and AND'ed i.e. $(A+B)' = A' \cdot B'$

2. two separate term Nanded together is same as the two term inverted (Complement and OR' ed. i.e

$$(A \cdot B)' = A' + B'$$

$$\begin{aligned}
 1. & A'B'C' + A'BC' + AB'C' + ABC' \\
 \Rightarrow & A'C'(B'+B) + AC'(B'+B) \\
 \Rightarrow & A'C'(1) + AC'(1) \quad \because B'+B=1 \\
 \Rightarrow & C'(A'+A) \quad \because A'+A=1 \\
 \Rightarrow & C' \quad \text{Answer}
 \end{aligned}$$

$$\begin{aligned}
 2. & (A+B+C)(A+B'+C')(A+B+C')(A+B'+C) \\
 \Rightarrow & (AA+AB'+AC'+BA+BB'+BC'+AC+BC+C'C) \\
 & \cdot (AA+AB'+AC+AB+B'B+BC+AC'+B'C'+C'C) \\
 \Rightarrow & (A+AB'+AC'+AB+BC'+AC+B'C) \cdot (A+AB'+AC+AB+BC+AC'+B'C) \\
 \Rightarrow & (A(1+B') + AC' + AB + BC' + AC + B'C) \cdot (A(1+B') + AC + AB + BC + AC' + B'C) \\
 \Rightarrow & (A(1+B) + AB + BC' + AC + B'C) (A(1+C) + AB + BC + AC' + B'C') \\
 \Rightarrow & (A(1+B) + BC' + AC + B'C) (A(1+B) + BC + AC' + B'C') \\
 \Rightarrow & (A(1+C) + BC' + B'C) (A(1+C') + BC + B'C') \\
 \Rightarrow & (A + BC' + B'C) (A + BC + B'C') \\
 \Rightarrow & (AA + ABC + AB'C' + ABC' + BCBC' + BCB'C + AB'C + BCB'C + B'C B'C') \\
 \Rightarrow & (A + ABC + AB'C' + ABC' + AB'C) \\
 \Rightarrow & (A + ABC + AB'C + AB'C' + ABC') \\
 \Rightarrow & (A + AC(B+B') + AC'(B'+B)) \\
 \Rightarrow & (A + AC + AC') \\
 \Rightarrow & (A + A(C+C')) \\
 \Rightarrow & (A + A) \\
 \Rightarrow & A \quad \text{Answer}
 \end{aligned}$$

3. What are universal gates? Why are they called so?

Answer → A Universal gate is a gate which can implement any boolean funⁿ. without need of any other gate. the NAND and NOR are called Universal gates.

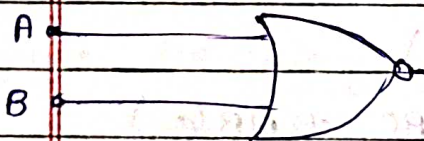
• NAND gate → This is NOT-AND Gate. the output of NAND gate is high (1) if any of the input is low.



Truth Table

A	B	$Y = A \cdot \bar{B}$
0	0	1
0	1	1
1	0	1
1	1	0

• NOR gate → This is NOT-OR gate. the output of NOR gate is low if any one of the input is high.



Truth Table

A	B	$Y = \overline{A+B}$
0	0	1
0	1	0
1	0	0
1	1	0

Draw the logic dia of EX-OR gate using universal gate?

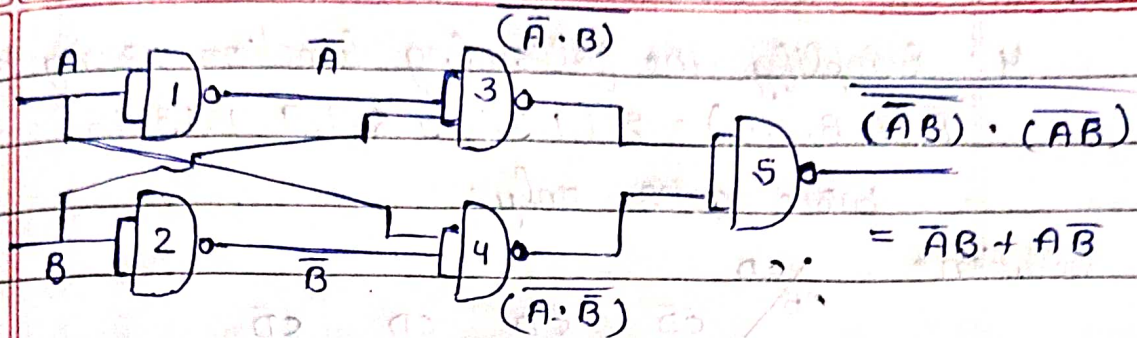
Sol → EX-OR Using NAND Gate

Method
1st

$$Y = \bar{A}B + A\bar{B}$$

$$Y = \overline{\bar{A}B + AB} \quad [\because \bar{\bar{A}} = A]$$

$$\Rightarrow \overline{(\bar{A}B) \cdot (AB)}$$



Ex-OR Gate Using NOR Gate:-

$$Y = \bar{A}B + A\bar{B} + A \cdot \bar{A} + B \cdot \bar{B}$$

$$= \bar{A}(A+B) + \bar{B}(A+B)$$

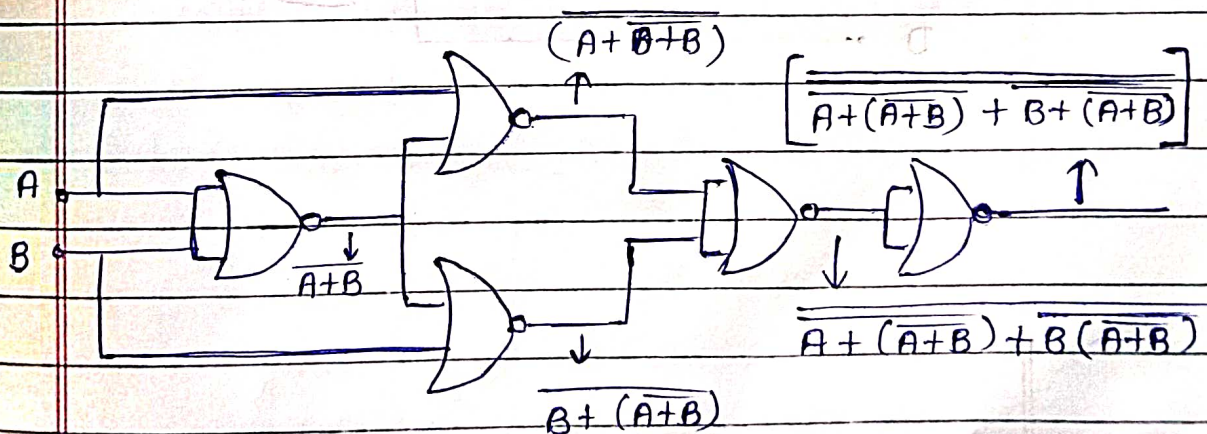
$$\Rightarrow \overline{A \cdot (A+B) + \bar{B} \cdot (A+B)}$$

$$\Rightarrow \overline{[\bar{A}(A+B)] \cdot [\bar{B}(A+B)]}$$

$$\Rightarrow \overline{[\bar{A} + \overline{A+B}] \cdot [\bar{B} + \overline{A+B}]}$$

$$\Rightarrow \overline{[A + \overline{A+B}] + [\bar{B} + \overline{A+B}]}$$

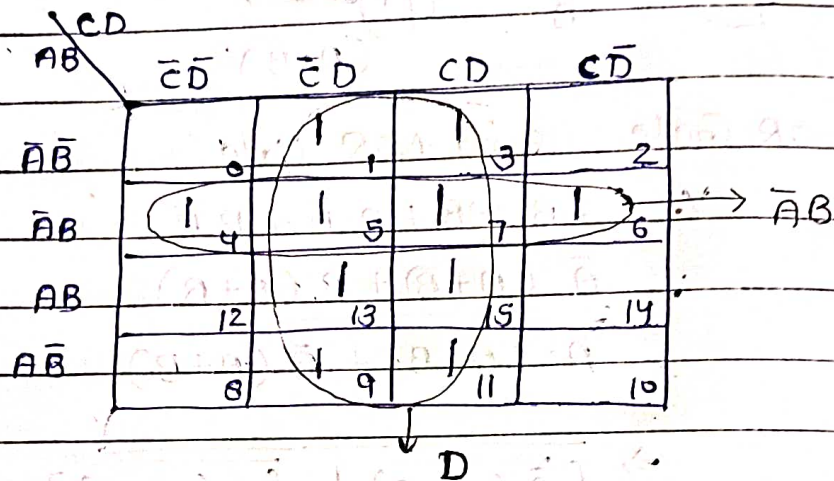
$$\Rightarrow \overline{[A + (\bar{A} + B)] + [B + (\bar{A} + B)]}$$



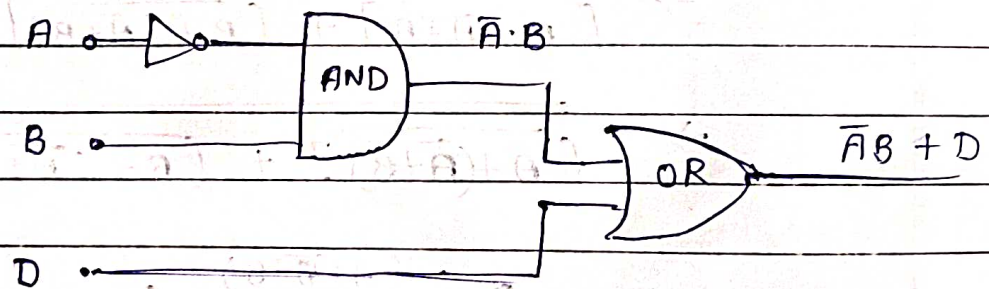
4. Simplify the following function using K-Map
 $F(A, B, C, D) = \sum (1, 3, 4, 5, 6, 7, 9, 11, 13, 15)$

— basic gates only.

Solution →



$$F(A, B, C, D) = \bar{A} \cdot B + D$$



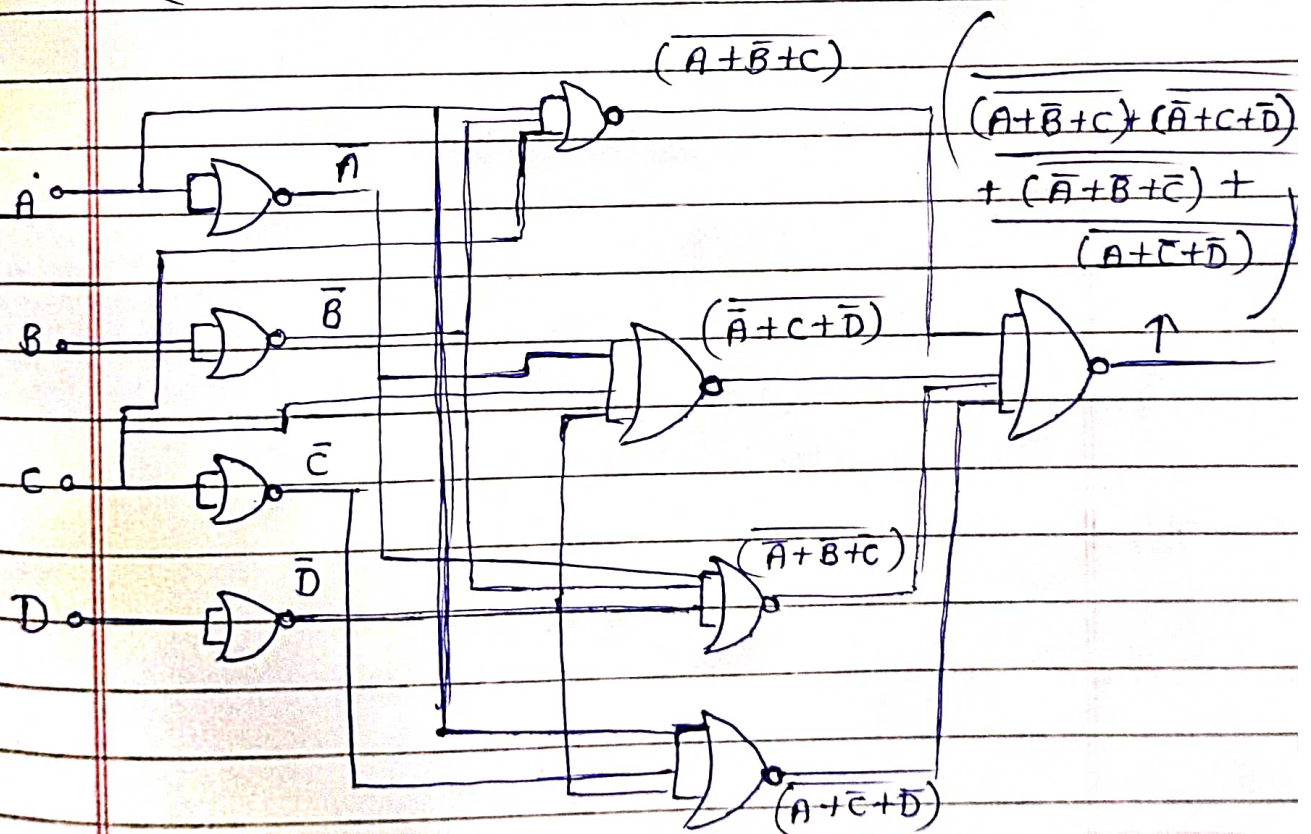
5. Minimize Using K-Map and realize using NOR Gate only.

$$F(A, B, C, D) = \Sigma(1, 3, 4, 5, 6, 7, 9, 13, 14, 15) \cdot d(0, 2, 8)$$

Solution → this is POS Condition. So there are Minterms then. $A=0$ & $\bar{A}=1$.

	$C+D$	$C+\bar{D}$	$\bar{C}+\bar{D}$	$\bar{C}+D$
$A+B$	X 0	1	0 3	X 2
$A+\bar{B}$	0 4	0 5	0 7	6
$\bar{A}+\bar{B}$	12	0 13	0 15	0 14
$\bar{A}+B$	X 8	0 9	11	10

$(A+\bar{B}C)$ $(\bar{A}+C+\bar{D})$



$$F = (A+\bar{B}+C) \cdot (\bar{A}+C+\bar{D}) \cdot (\bar{A}+\bar{B}+\bar{C}) \cdot (A+\bar{C}+\bar{D})$$

Answer

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(Assignment - 4) (Unit - 4)

1. A sample of water was found to contain
 $40.5 \text{ mg/l} = \text{Ca}(\text{HCO}_3)_2 = 46.5 \text{ mg/l} = \text{Mg}(\text{HCO}_3)_2$
 $32.1 \text{ mg/l} = \text{CaSO}_4$, $27.6 \text{ mg/l} = \text{MgSO}_4$, 22.5 mg/l
 $= \text{CaCl}_2$, $19.0 \text{ mg/l} = \text{MgCl}_2$. Calculate the temp.
hardness of water sample?

Answer:

Impurity	Quantity	Eq. wt	Hardness
$\text{Ca}(\text{HCO}_3)_2$	40.5	81	$\Rightarrow 40.5 \times \frac{50}{81} = 25$
$\text{Mg}(\text{HCO}_3)_2$	46.5	73	$\Rightarrow 46.5 \times \frac{50}{73} = 31.8$
CaSO_4	32.1	68	$\Rightarrow 32.1 \times \frac{50}{68} = 23.6$
MgSO_4	27.6	60	$\Rightarrow 27.6 \times \frac{50}{60} = 23$
CaCl_2	22.5	55.5	$\Rightarrow 22.5 \times \frac{50}{55.5} = 20.27$
MgCl_2	19.0	47.5	$\Rightarrow 19 \times \frac{50}{47.5} = 20$

Temporary Hardness

due to $(\text{Mg}(\text{HCO}_3)_2 + \text{Ca}(\text{HCO}_3)_2)$

$$\Rightarrow 25 + 31.8 = 56.8 \text{ ppm}$$

Permanent Hardness

due to $(\text{CaSO}_4 + \text{MgSO}_4 + \text{CaCl}_2 + \text{MgCl}_2)$

$$\Rightarrow 23.60 + 23 + 20.27 + 20$$

$$\Rightarrow 86.87 \text{ ppm}$$

Total Hardness = Temporary + Permanent

$$\Rightarrow 56.8 + 86.87$$

$$\Rightarrow 143.67 \text{ ppm} \quad \text{Answer}$$

2- what do you mean by term permutit?

Explain zeolite process for water softening?

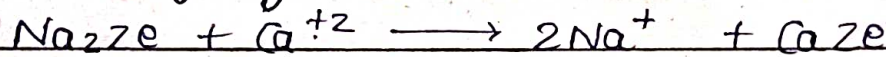
Numerical • A Zeolite softener ----- Sample

Answer The word permutit means boiling stone.

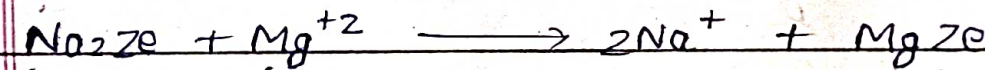
Zeolites are hydrated Sodium alumina silicates. They have porous structure with molecular formula $\text{Na}_2\text{O} \cdot \text{Al}_2\text{O}_3 \cdot x \text{SiO}_2 \cdot y \text{H}_2\text{O}$
 $x = 2 \text{ to } 10 + y = 2 \text{ to } 6$.

Represented as Na_2Ze (Ze = thumsoluble framework: Na = loosely held Sodium ions)

• Water softing



(Zeolite) (Calcium Salts) (Released Salts in water) (Calcium Zeolite)



(Zeolite) (Magnesium Salts) (Released in water) (Magnesium Zeolite)

Imp. Quantity Eq.wt $\text{CaCO}_3 \text{ Eq}^n$ (Mg/L) L or S

Ca^{+2}	160	20	$160 \times \frac{50}{20} = 400$	S
Ca_2	48	22	$48 \times \frac{50}{22} = 150$	L+S
HCO_3^-	66	61	$264 \times \frac{50}{61} = 216.39$	L
H^+	264	1	$20 \times \frac{50}{1} = 100$	L-S
CO_3^{-2}	20	30	$45 \times \frac{50}{30} = 75$	L+S
OH^-	45	17	$68 \times \frac{50}{17} = 200$	L+S
NaHCO_3	10	82	$10 \times \frac{50}{82} = 6.09$	- L+S
NaCl	4.7	-	NO Hardness	-

$$\text{lime} = \frac{74}{100} \left[\text{Mg}^{+2} + \text{CO}_2 + \text{HCO}_3^- + \text{H}^+ - \text{NaHCO}_3 \right] \times \frac{100}{\% \text{ Purity}}$$

$$\Rightarrow \frac{74}{100} \left[200 + 150 + 216 \cdot 39 + 100 - 6 \cdot 09 \right] \times \frac{100}{74} \times \frac{125\%}{106}$$

$$\Rightarrow 107.53 \text{ Kg}$$

$$\text{Soda} = \frac{106}{100} \left[\text{Ca}^{+2} + \text{Mg}^{+2} \cdot \text{HCO}_3^- + \text{CO}_3^{+2} + \text{OH}^- \right] \times \frac{100}{\% \text{ Purity}}$$

$$\Rightarrow \frac{106}{100} \left[400 + 200 - 216 \cdot 39 + 200 + 75 \right] \times \frac{106}{94} \times \frac{125\%}{106}$$

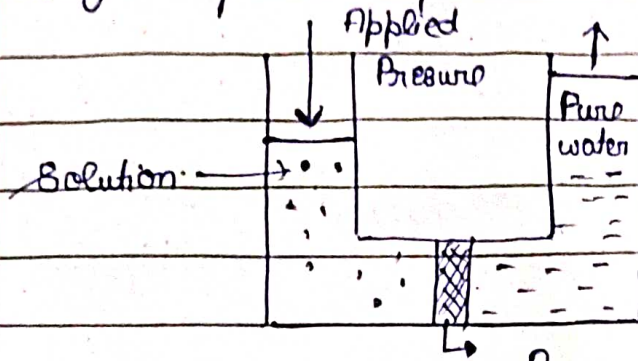
$$\Rightarrow 97.39 \text{ Kg}$$

3- write a short note on Reverse Osmosis?

Answer: Osmosis $\rightarrow$ is a process to demineralize water by pushing it under pressure through a semi permeable membrane from the lower concentration to the higher concentration.

Reverse Osmosis $\rightarrow$ Pressure higher than osmotic pressure is applied from the higher concentration side so that solvent moves from higher concentration to lower concentration; Reverse Osmosis or Super filtration is a water purification process that uses a partially permeable membrane to remove ions unwanted molecules &

Larger particles ^{are} pushing water



Permeable membrane

4- Calculate the minimum weight of air required for complete combustion of 1 kg of fuel containing C = 90% — rest.

Solution →

$$C = 90\% \text{ of } 1 \text{ kg} \\ = \frac{90}{100} \times 1000 \text{ g} = 900 \text{ g}$$

$$H = 3.5\% \text{ of } 1 \text{ kg} = 35 \text{ g}$$

$$O = 3\% \text{ of } 1 \text{ kg} = 30 \text{ g}$$

$$S = 5 \text{ g}$$

$$H_2O = 10 \text{ g}$$

$$N = 5 \text{ g}$$

$$\text{Net } O_2 \Rightarrow \left[\frac{32}{12} C + 8H + S - O \right]$$

$$\Rightarrow \frac{32}{12} \times 900 + 8 \times 35 + 5 - 30$$

$$\Rightarrow 2400 + 280 + 5 - 30$$

$$\Rightarrow 2655 \text{ g}$$

$$\text{Weight of air required} = \frac{\text{Net } O_2 \times 100}{23}$$

$$\Rightarrow \frac{2655 \times 100}{23}$$

$$\Rightarrow 11543.47 \text{ g} \quad \underline{\text{Answer}}$$

5- A sample of coal contains C = 93%, H = 6%,
 Ash = 1%. The following data was obtain-
 ed when the above coal was tested in Bomb's
 Calorimetry Bomb - - - - - Steam = 580 cal/g

Solution -

$$HCV = \frac{(W+10)(t_2 - t_1) - (CA + P)}{x}$$

$$\Rightarrow \frac{(2200 + 580)(24.2 - (50 + 10))}{0.92}$$

$$\Rightarrow 7168.48 \text{ Cal/gm}$$

$$LCV = GCV - 0.09 \times \%H \times \text{Latent heat of Steam}$$

$$\Rightarrow 7168.4782 - 0.09 \times 6 \times 580$$

$$\Rightarrow 6855.28 \text{ Cal/gm. } \underline{\text{Answer}}$$